

# Flavor changing scalar couplings and $t\gamma(Z)$ production at hadron colliders

Chong-Xing Yue and Zheng-Jun Zong

Department of Physics, Liaoning Normal University, Dalian, 116029. P. R. China \*

February 2, 2008

## Abstract

We calculate the contributions of the flavor changing scalar ( $FCS$ ) couplings arising from topcolor-assisted technicolor ( $TC2$ ) models at tree-level to the  $t\gamma$  and  $tZ$  production at the Tevatron and  $LHC$  experiments. We find that the production cross sections are very small at the Tevatron with  $\sqrt{s} = 1.96TeV$ , which is smaller than 5 fb in most of the parameter space of  $TC2$  models. However, the virtual effects of the  $FCS$  couplings on the  $t\gamma(Z)$  production can be easily detected at the  $LHC$  with  $\sqrt{s} = 14TeV$  via the final state  $\gamma l\bar{\nu}b$  ( $l^+l^-l\bar{\nu}b$ ).

---

\*E-mail: cxyue@lnnu.edu.cn

## I. Introduction

The top quark, with a mass of the order of the electroweak symmetry breaking(*EW**SB*) scale  $m_t \approx 178.0 \pm 4.36 \text{ GeV}$ [1], is singled out to play a key role in probing the new physics beyond the standard model(*SM*). The properties of the top quark could reveal information regarding flavor physics, *EW**SB* mechanism, as well as new physics beyond the *SM*[2]. Hadron colliders, such as the Tevatron and the *CERN LHC*, can be seen as top quark factories. One of the primary goals for the Tevatron and the *LHC* is to accurately determine the top quark properties, and to see whether any hint of non-standard physics may be visible.

The anomalous top quark couplings  $tqv$  ( $q = c\text{-or } u\text{-quarks}$  and  $v = \gamma, Z, \text{ or } g$  gauge bosons), which arise from the flavor changing (*FC*) interactions, can affect top production and decay at high energy collider as well as precisely measured quantities with virtual top contributions. In the *SM*, this type of couplings vanish at the tree-level but can be generated at the one-loop level. However, they are suppressed by the *GIM* mechanism, which can not be detected in the present and near future high energy experiments[3]. Thus, any signal indicating this type of couplings is evidence of new physics beyond the *SM* and will shed more light on flavor physics in the top quark sector.

Single top quark production is very sensitive to the anomalous top coupling  $tqv$ , which can be generated in supersymmetry, topcolor scenario, and other specific models beyond the *SM*. Thus, studying the contributions of this type of couplings to single top production is of special interest. This fact has led to many studies involving single top production via the  $tqv$  couplings in lepton colliders[4,5] and hadron colliders[6,7,8].

To completely avoid the problems arising from the elementary Higgs field in the *SM*, various kinds of dynamical *EW**SB* models have been proposed, and among which the topcolor scenario is attractive because it can explain the large top quark mass and provide possible *EW**SB* mechanism[9]. Almost all of this kind of models propose that the scale of the gauge groups should be flavor non-universal. When one writes the non-universal interactions in the mass eigen-basis, it can induce the tree-level *FC* couplings. For example, the top-pions  $\pi_t^{\pm,0}$  predicted by topcolor scenario have large Yukawa couplings

to the third family quarks and can induce the tree-level flavor changing scalar ( $FCS$ ) couplings[10], which have significant contributions to the anomalous top couplings  $tqv$ [5]. The aim of this paper is to calculate the contributions of the  $FCS$  coupling  $\pi_t^0 \bar{t}c$  to the processes  $gc \rightarrow t\gamma$  and  $gc \rightarrow tZ$  in the framework of topcolor-assisted technicolor (TC2) models[11], and see whether the effects of the  $FCS$  coupling  $\pi_t^0 \bar{t}c$  on  $t\gamma$  and  $tZ$  production can be detected at the Tevatron and the  $LHC$  experiments.

## II. The calculations of $t\gamma(Z)$ production in TC2 models

For TC2 models[9,11], the underlying interactions, topcolor interactions, are assumed to be chiral critically strong at the scale about  $1TeV$  and coupled preferentially to the third generation, and therefore do not possess  $GIM$  mechanism. This is an essential feature of this kind of models due to the need to single out top quark for condensate. The non-universal gauge interactions result in the mass eigen-basis, which can induce the anomalous top quark couplings  $tuv$  and  $tcv$ . However, the  $tuv$  couplings can be neglected because the  $FCS$  coupling  $\pi_t^0 \bar{t}u$  is very small[10]. The effective forms of the anomalous coupling vertices  $\Lambda_{tcZ}$ ,  $\Lambda_{tc\gamma}$ , and  $\Lambda_{tcg}$  can be writted as[5]:

$$\Lambda_{tcZ}^\mu = ie[\gamma^\mu(F_{1Z} + F_{2Z}\gamma^5) + p_t^\mu(F_{3Z} + F_{4Z}\gamma^5) + p_c^\mu(F_{5Z} + F_{6Z}\gamma^5)], \quad (1)$$

$$\Lambda_{tc\gamma}^\mu = \Lambda_{tcZ}^\mu|_{F_{iZ} \rightarrow F_{i\gamma}}, \quad \Lambda_{tcg}^\mu = ig_s \frac{\lambda^a}{2} [\gamma^\mu F_{1g} + p_t^\mu F_{2g} + p_c^\mu F_{3g}] \quad (2)$$

with

$$F_{i\gamma} = F_{iZ}|_{v_t=\frac{2}{3}, a_t=0}, \quad F_{ig} = \frac{3}{2}F_{i\gamma}. \quad (3)$$

Where  $\lambda^a$  is the Gell-Mann matrix. The form factors  $F_{iv}$  are expressed in terms of two - and three - point standard Feynman integrals[12]. The expressions of  $F_{iZ}$  are given in Ref.[5].

Obviously, the  $FCS$  coupling  $\pi_t^0 \bar{t}c$  can generate contributions to the processes  $g(p_g) + c(p_c) \rightarrow t(p_t) + \gamma(p_\gamma)$  and  $g(p_g) + c(p_c) \rightarrow t(p'_t) + Z(p_Z)$  via the anomalous top quark couplings  $tc\gamma$ ,  $tcZ$ , and  $tcg$ . The relevant Feynman diagrams are shown in Fig.1, in which Fig.1(a) and Fig.1(b) come from the anomalous  $tc\gamma$  and  $tcZ$  couplings, while Fig.1(c) and Fig.1(d) come from the anomalous  $tcg$  coupling. The renormalized amplitudes for these

processes have similar forms with those of the process  $\gamma p \rightarrow \gamma c \rightarrow t\gamma(Z)$ , which have been given in Ref.[8].

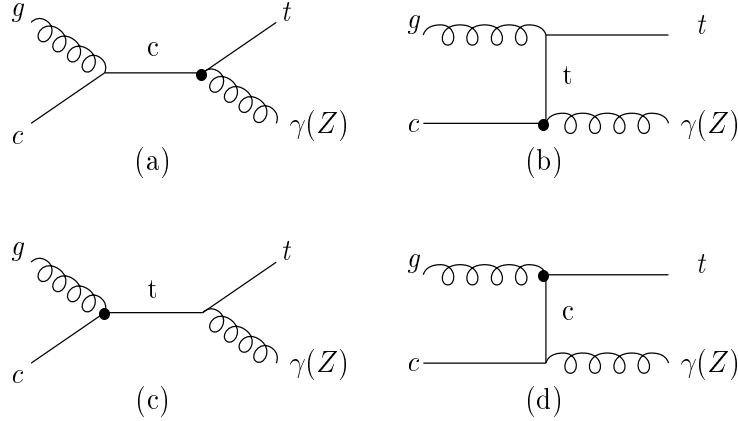


Figure 1: Feynman diagrams for  $t\gamma(Z)$  production contributed by the anomalous top coupling vertices  $\Lambda_{tc\gamma}$ ,  $\Lambda_{tcZ}$ , and  $\Lambda_{tcg}$ .

After calculating the partonic cross sections  $\hat{\sigma}_i(\hat{s})$  for the subprocesses  $gc \rightarrow t\gamma$  and  $gc \rightarrow tZ$ , the total cross sections  $\sigma_i(s)$  at hadron coliders are obtained by convoluting  $\hat{\sigma}_i(\hat{s})$  with the parton distribution functions  $f_{c/p}(x_1, Q)$  and  $f_{g/p}(x_2, Q)$  of the initial state particles  $c$  and  $g$ :

$$\sigma_i(s) = \int \int dx_1 dx_2 f_{c/p}(x_1, Q) f_{g/p}(x_2, Q) \hat{\sigma}_i(\hat{s}), \quad (4)$$

where  $\hat{s} = xs$ , and  $x = x_1 x_2$ . In our calculation, we will take the CTEQ5 parton distribution function for  $f_{c/p}(x_1, Q)$  and  $f_{g/p}(x_2, Q)$  with  $Q^2 = \hat{s}$ [13].

### III. Numerical results and conclusions

From above equations, we can see that the cross sections of  $t\gamma$  and  $tZ$  production at the Tevatron and the  $LHC$  are dependent on two free parameters  $\varepsilon$  and  $m_{\pi_t}$  of  $TC2$  models, except the  $SM$  input parameters  $\alpha_e$ ,  $\alpha_s$ ,  $S_W$ ,  $m_Z$  and  $m_t$ . In  $TC2$  models, topcolor interactions make small contributions to  $EW\!SB$  and give rise to the main part

of the top quark mass,  $(1 - \varepsilon)m_t$  with  $0.01 \leq \varepsilon \leq 0.1$ , a model dependent free parameter. The limits on the top-pion mass  $m_{\pi_t}$  may be obtained via studying its effects on various observables[9]. It has been shown that  $m_{\pi_t}$  is allowed to be in the range of a few hundred  $GeV$  depending on the models. As numerical estimation, we will assume  $m_{\pi_t}$  and  $\varepsilon$  in the ranges of  $200GeV \sim 400GeV$  and  $0.01 \sim 0.1$ , respectively.

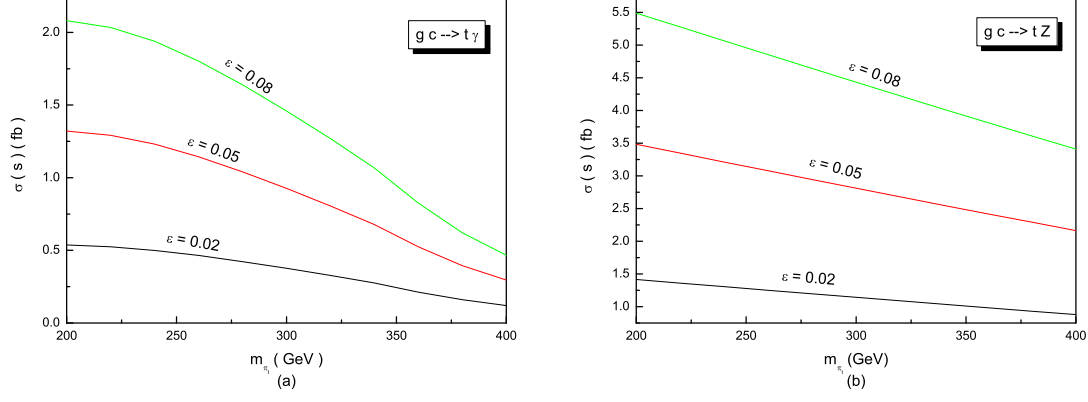


Figure 2: The cross section  $\sigma(s)$  of  $t\gamma(Z)$  production as a function of the top-pion mass  $m_{\pi_t}$  for three values of the parameter  $\varepsilon$  at the Tevatron with  $\sqrt{s} = 1.96TeV$

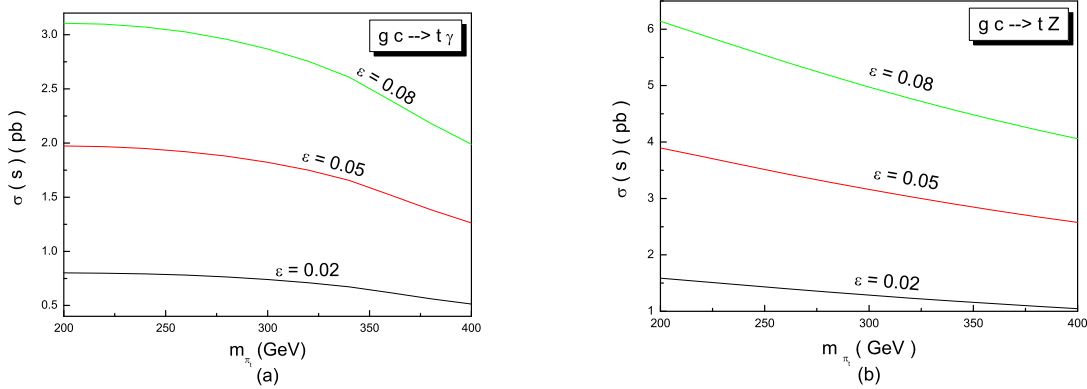


Figure 3: The cross section  $\sigma(s)$  of  $t\gamma(Z)$  production as a function of  $m_{\pi_t}$  for three values of the parameter  $\varepsilon$  at the  $LHC$  with  $\sqrt{s} = 14TeV$

The cross sections  $\sigma_i(s)$  of  $t\gamma(Z)$  production at the Tevatron with  $\sqrt{s} = 1.96TeV$  and  $LHC$  with  $\sqrt{s} = 14TeV$  are plotted as functions of the neutral top-pion mass  $m_{\pi_t}$  for

three values of the free parameter  $\varepsilon$  in Fig.2 and Fig.3, respectively. From these figures, we can see that the  $t\gamma$  production cross section is smaller than  $tZ$  production cross section at the same collider experiment. This is because the effective coupling strength of  $\Lambda_{tc\gamma}$  is smaller than that of  $\Lambda_{tcZ}$  and the c. m. energy  $\sqrt{s} \gg m_Z$ . For  $200\text{GeV} \leq m_{\pi_t} \leq 400\text{GeV}$  and  $0.02 \leq \varepsilon \leq 0.08$ , the cross sections of  $t\gamma$  and  $tZ$  production at the Tevatron are in the ranges of  $1.2 \times 10^{-4}\text{pb} \sim 2.1 \times 10^{-3}\text{pb}$  and  $8.8 \times 10^{-4}\text{pb} \sim 5.4 \times 10^{-3}\text{pb}$ , respectively. If we assume the yearly integrated luminosity  $\mathcal{L}_{int} = 2\text{fb}^{-1}$  for the Tevatron with  $\sqrt{s} = 1.96\text{TeV}$ , then the number of the yearly production events is smaller than 10 in almost of all parameter space of  $TC2$  models. Thus, it is very difficult to detect the effects of the  $FCS$  coupling  $\pi_t^0 \bar{t}c$  on the  $t\gamma$  and  $tZ$  production at the Tevatron experiments. However, it is not this case for the future  $LHC$  experiment with  $\sqrt{s} = 14\text{TeV}$  and  $\mathcal{L}_{int} = 100\text{fb}^{-1}$ . There will be  $3.1 \times 10^5 \sim 5.1 \times 10^4$   $t\gamma$  events and  $6.1 \times 10^5 \sim 1.0 \times 10^5$   $tZ$  events to be generated per year.

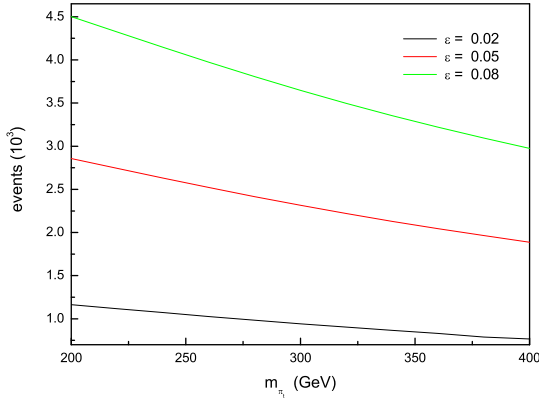


Figure 4: The number of the  $l^+l^-l\bar{\nu}b$  events generated at the  $LHC$  with  $\sqrt{s} = 14\text{TeV}$  is showed as a function of  $m_{\pi_t}$  for three values of the parameter  $\varepsilon$

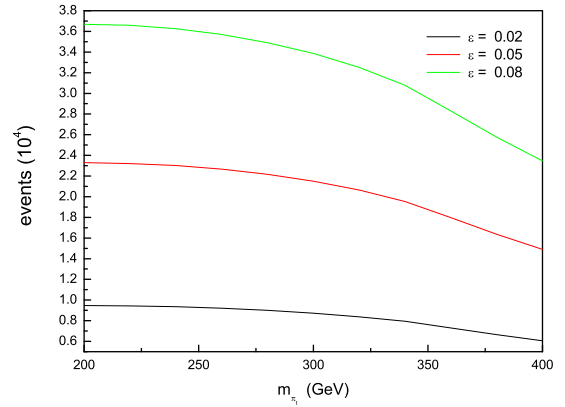


Figure 5: The number of the  $\gamma l\bar{\nu}b$  events generated at the  $LHC$  with  $\sqrt{s} = 14\text{TeV}$  is showed as a function of  $m_{\pi_t}$  for three values of the parameter  $\varepsilon$

In general  $tZ$  production gives the possible observable five fermion final states with at least one  $b$  quark  $fffb$  including  $\nu\bar{\nu}jjb$  with  $Z \rightarrow \nu\bar{\nu}$  and  $W \rightarrow q\bar{q}'$ ,  $jjl\nu b$  with  $Z \rightarrow q\bar{q}'$  and  $W \rightarrow l\bar{\nu}$ , etc. It has been shown that the final state  $\nu\bar{\nu}jjb$  with branching ratio  $B_r(tZ \rightarrow \nu\bar{\nu}jjb) \approx 13\%$  is the best signal event for detection the new physics effects

on  $tZ$  production at the Tevatron with  $\sqrt{s} = 1.96\text{TeV}$  and  $\mathcal{L}_{int} = 2fb^{-1}$ [14]. Although the final states  $b\bar{b}l\bar{\nu}b$  and  $l^+l^-\bar{l}\nu b$  have smaller branching ratios  $B_r(tZ \rightarrow b\bar{b}l\bar{\nu}b) \approx 3.3\%$  and  $B_r(tZ \rightarrow l^+l^-\bar{l}\nu b) \approx 1.5\%$ , they are the most interesting modes at the  $LHC$  with  $\sqrt{s} = 14\text{TeV}$  and  $\mathcal{L}_{int} = 100fb^{-1}$ , due to smaller backgrounds. In Fig.4, we plot the number of the signal event  $l^+l^-\bar{l}\nu b$  at the  $LHC$  as a function of  $m_{\pi_t}$  for three values of the free parameter  $\varepsilon$ . In this figure, we have taken the experimental efficiency  $\epsilon$  for detection the final state fermions as the commonly used reference values:  $\epsilon = 95\%$  for leptons and  $\epsilon = 60\%$  for  $b$  quark. One can see from Fig.4 that, in most of the parameter space of  $TC2$  models, there will be several hundreds and up to thousands observed  $l^+l^-\bar{l}\nu b$  events to be generated at the  $LHC$  experiments. Thus, the virtual effects of the  $FCS$  coupling  $\pi_t^0\bar{t}c$  on  $tZ$  production should be detected in the future  $LHC$  experiments.

Compared with those of  $tZ$  production, the final states with a photon and three fermions of  $t\gamma$  production are very simply, only  $\gamma l\bar{\nu}b$  and  $\gamma jjb$  depending whether the  $SM$  gauge boson  $W$  decays into leptons or hadrons. The leptonic final state  $\gamma l\bar{\nu}b$  has a branching ratio  $B_r(t\gamma \rightarrow \gamma l\bar{\nu}b) \approx 21.8\%$  and the hadronic final state  $\gamma jjb$  has a branching ratio  $B_r(t\gamma \rightarrow \gamma jjb) \approx 67.8\%$ . The  $\gamma l\bar{\nu}b$  final state is the most interesting signal event, due to its small  $\gamma Wj$  background[14]. The number of the observed  $\gamma l\bar{\nu}b$  events is plotted in Fig.5 as a function of  $m_{\pi_t}$  for three values of the parameter  $\varepsilon$ . One can see from Fig.5 that the number of the observed  $\gamma l\bar{\nu}b$  events are larger than that of the observed  $l^+l^-\bar{l}\nu b$  events for  $tZ$  production in all of the parameter space. So, the  $FCS$  coupling  $\pi_t^0\bar{t}c$  can be more easy detected via the  $t\gamma$  production process than via the  $tZ$  production at the  $LHC$  experiments.

$TC2$  models also predict the existence of the neutral scalar top-Higgs  $h_t^0$ , which is a  $t\bar{t}$  bound and analogous to the  $\sigma$  particle in low energy  $QCD$ . Similar to the neutral top-pion  $\pi_t^0$ , it can also give rise to the large effective  $tc\gamma$  and  $tcZ$  couplings via the  $FCS$  coupling  $h_t^0\bar{t}c$ . Our explicit calculation shows that the effect of the  $FCS$  coupling  $h_t^0\bar{t}c$  on the  $t\gamma(Z)$  production is similar to that of the  $FCS$  coupling  $\pi_t^0\bar{t}c$ .

In many of the extensions of the  $SM$ , the  $GIM$  mechanism does not work so well as in the  $SM$ . The top quark  $FC$  interactions might be predicted in supersymmetry, topcolor

scenario, and other specific models beyond the  $SM$ , which can generate significantly contributions to rare top decays and single top production processes[2,15]. Thus, these interactions can lead to observable effects in various high energy colliders[16]. For example, the large anomalous top couplings  $tcv$  generated by the tree-level  $FCS$  couplings  $\pi_t^0\bar{t}c$  or  $h_t^0\bar{t}c$  can enhance the branching ratios of the rare top decays  $t \rightarrow cv$ [17] and the cross sections of single top production at high energy  $e^+e^-$  collider( $LC$ )[5] and the  $ep$  colliders[8]. In the context of  $TC2$  models, the  $FCS$  couplings  $\pi_t^0\bar{t}c$  and  $h_t^0\bar{t}c$  make the cross section of the process  $e^+e^- \rightarrow \bar{t}c$  in the range of  $0.014fb \sim 0.35fb$  at the  $LC$  experiment with  $\sqrt{s} = 500GeV$  and that of the process  $ep \rightarrow \gamma c \rightarrow t\gamma(tZ)$  in the range of  $0.14pb \sim 1.37pb(0.13pb \sim 1.35pb)$  at the  $THERA$  collider with  $\sqrt{s} = 1000GeV$ , which may be detected in these future collider experiments. Furthermore, Ref.[17] has shown that, in most of the parameter space of  $TC2$  models, there are  $B_r(t \rightarrow c\gamma) \sim 1 \times 10^{-6}$ ,  $B_r(t \rightarrow cZ) \sim 1 \times 10^{-4}$  and  $B_r(t \rightarrow cg) \sim 1 \times 10^{-4}$ . At the  $LHC$  experiment with  $\sqrt{s} = 14TeV$  and  $\mathcal{L}_{int} = 100fb^{-1}$ , the production cross section of the top quark pairs via standard  $QCD$  interactions is about  $8 \times 10^5fb$ . If we assume that the top quark decays via  $t \rightarrow cv$  with  $Z \rightarrow e^+e^-$  and the antitop quark decays via  $\bar{t} \rightarrow W^-\bar{b}$  with  $W^- \rightarrow l^-\bar{\nu}_l$ , then, at most, there are several hundreds observable events to be generated per year. Thus, the virtual effects of the  $FCS$  couplings  $\pi_t^0\bar{t}c$  or  $h_t^0\bar{t}c$  can be more easy detected via the  $t\gamma(Z)$  production process than via the rare top decays  $t \rightarrow cv$  at the  $LHC$  experiments.

Topcolor scenario is one of the important candidates for the mechanism of  $EWSB$ . A key feature of this kind of models is that topcolor interactions are assumed to couple preferentially to the third generation and there do not posses  $GIM$  mechanism. The non-universal gauge interactions can induce the  $FCS$  couplings  $\pi_t^0\bar{t}c$  and  $h_t^0\bar{t}c$ . If the virtual effects of the  $FCS$  couplings can indeed be detected at the  $LHC$  experiments, it will be helpful to test topcolor scenario and understand  $EWSB$  mechanism.

## Acknowledgments

Z. J. Zong would like to thank Bin Zhang for helpful discussions. This work was supported in part by the National Natural Science Foundation of China under the grant



## References

- [1] P. Azzi et al. [*CDF* and D0 Collaborations and Tevatron Electroweak Working Group], *hep-ex/0404010*; V. M. Abazov et al. [D0 Collaboration], *Nature* **429**(2004)638.
- [2] For reviews see : M. Beneke ,et al., Top quark physics, *hep-ph/0003033*; E. H. Simmons, Top physics, *hep-ph/0011244*.
- [3] G. Eilam, J. L. Hewett, A. Soni, *Phys. Rev. D***44**(1991)1473.
- [4] K. J. Abraham, K. Whisnant, B. - L. Young, *Phys. Lett. B***419**(1998)381; V. F. Obraztsov, S. R. Slabospitsky, O. P. Yushchenko, *Phys. Lett. B***426**(1998)393; B. A. Arbuzov, M. Yu. Osipov, *hep-ph/9802392*; T. Han, J. L. Hewett, *Phys. Rev. D***60**(1999)074051; S. Bar-Shalom, J. Wudka, *Phys. Rev. D***60**(1999)094916; J. A. Aguilar-Saavedra, *Phys. Lett. B***502**(2001)115; J. A. Aguilar-Saavedra, T. Riemann, *hep-ph/0102197*; J. J. Cao, Z. H. Xiong, J. M. Yang, *Nucl. Phys. B***651**(2003)87; J. J. Cao, G. L. Liu, J. M. Yang, *hep-ph/0311166*; Chong-Xing Yue et al , *Phys. Lett. B***496**(2000)93.
- [5] Chong-Xing Yue, Yuan-Ben Dai, Qing-Jun Xu, Guo-Li liu, *Phys. Lett. B***525**(2002)301.
- [6] E. Malkawi, T. Tait, *Phys. Lett. D***54**(1996)5758; T. Han, et al., *Phys. Lett. B***385**(1996)311; T. Tait, C.-P. Yuan, *Phys. Lett. B***55**(1997)7300; M. Hosch, K. Whisnant, B.-L. Young ,*Phys. Rev. D***56**(1997)5725; T. Han, et al., *Phys. Rev. D***58**(1998)073008; T. Tait, C.-P. Yuan, *Phys. Rev. D***63**(2000)014018; F. del Aguila, J. A. Aguilar-Saavedra, *Phys. Lett. B***462**(1999)310; J. J. Cao, Z. H. Xiong, J. M. Yang, *Phys. Rev D***67**(2003)071701; N. Kidonakis and A. Belyaer, *hep-ph/0310299*.

- [7] A. Belyaev, N. Kidonakis, *Phys. Rev. D***65**(2002)037501; H. Fritzsch, D. Holtmannsp Ötter, *Phys. Lett. B***457**(1999)186; O.Cakir, S. Sultansoy, M. Yilmaz, *hep-ph/0105130*; A. T. Alan, A. Senol, *Europhys. Lett.* **59**(2002)669;
- [8] Chong-Xing Yue, Dong-Qi Yu, Zheng-Jun Zong, *Phys. Lett. B***591**(2004)220.
- [9] C. T. Hill, E. H. Simmons, *Phys. Rep.* **381**(2003)235, [Erratum -ibid, 390(2004)553].
- [10] H.-J. He, C.-P. Yuan, *Phys. Rev. Lett.* **83**(1999)28; G. Burdman, *Phys. Rev. Lett.* **83**(1999)2888.
- [11] C. T. Hill, *Phys. Lett. B***345**(1999)483; K. Lane, T. Eichten, *Phys. Lett. B***352**(1995)382; K. Lane, *Phys. Lett B***433**(1998)96; G. Cvetič, *Rev. Mod. Phys.* **71**(1999)513.
- [12] G. Passarino, M. Veltman, *Nucl. Phys. B***160**(1979)151; A. Axelrod, *Nucl. Phys. B* **209**(1982)349; M. Clements, *et al.*, *Phys. Rev. D***27**(1983)570.
- [13] CTEQ Collaboration, H. L. Lai, et al., *Eur. Phys.* **12**(2000)375; J. Pumplin, D. R. Stump, J. Huston, H. L. Lai, P. Nadolsky, W. K. Tung, *JHEP* **0207**(2002)012.
- [14] F. del Aguila, J. A. Aguilar-Saavedra, L1. Ametller, *Phys. Lett. B***462**(1999)310; F. del Aguila and J. A. Aguilar-Saavedra, *Nucl. Phys. B***576**(2000)56.
- [15] Jin-Min Yang, *hep-ph/0409351*.
- [16] J. A. Aguilar-Saavedra, *hep-ph/0409342*.
- [17] Chong-Xing Yue, *et al.*, *Phys. Rev. D***64**(2001)095004; Gong-Ru Lu, *et al.*, *Phys. Rev. D***68**(2003)015002.